

# 

### Semester Two Examination, 2017

### Question/Answer booklet

# MATHEMATICS

**SOLUTIONS**

**SPECIALIST**

**UNITS 1 AND 2**

## Section One:

## Calculator-free

|  |  |  |  |  |  |  |  |  |  |  |
| --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- |
| Student Number: In figures |  |  |  |  |  |  |  |  |  |  |

In words

Your name

## Time allowed for this section

Reading time before commencing work: five minutes

Working time: fifty minutes

## Materials required/recommended for this section

***To be provided by the supervisor***

This Question/Answer booklet

Formula sheet

***To be provided by the candidate***

Standard items: pens (blue/black preferred), pencils (including coloured), sharpener, correction fluid/tape, eraser, ruler, highlighters

Special items: nil

## Important note to candidates

No other items may be taken into the examination room. It is **your** responsibility to ensure that you do not have any unauthorised material. If you have any unauthorised material with you, hand it to the supervisor **before** reading any further.

## Structure of this paper

|  |  |  |  |  |  |
| --- | --- | --- | --- | --- | --- |
| Section | Number of questions available | Number of questions to be answered | Working  time (minutes) | Marks available | Percentage of examination |
| Section One:  Calculator-free | 8 | 8 | 50 | 52 | 35 |
| Section Two:  Calculator-assumed | 13 | 13 | 100 | 98 | 65 |
|  | | |  | **Total** | 100 |

## Instructions to candidates

1. The rules for the conduct of examinations are detailed in the school handbook. Sitting this examination implies that you agree to abide by these rules.

2. Write your answers in this Question/Answer booklet.

3. You must be careful to confine your response to the specific question asked and to follow any instructions that are specified to a particular question.

4. Additional working space pages at the end of this Question/Answer booklet are for planning or continuing an answer. If you use these pages, indicate at the original answer, the page number it is planned/continued on and write the question number being planned/continued on the additional working space page.

5. Show all your working clearly. Your working should be in sufficient detail to allow your answers to be checked readily and for marks to be awarded for reasoning. Incorrect answers given without supporting reasoning cannot be allocated any marks. For any question or part question worth more than two marks, valid working or justification is required to receive full marks. If you repeat any question, ensure that you cancel the answer you do not wish to have marked.

6. It is recommended that you do not use pencil, except in diagrams.

7. The Formula sheet is not to be handed in with your Question/Answer booklet.

Section One: Calculator-free 35% (52 Marks)

This section has**eight (****8)** questions. Answer **all** questions. Write your answers in the spaces provided.

Working time: 50 minutes.

Question 1 (6 marks)

(a) Determine the values of the real constants and if is a solution of the equation . (3 marks)

|  |
| --- |
| **Solution** |
|  |
| **Specific behaviours** |
| ✓ indicates other (conjugate) solution  ✓ states value of  ✓ states value of |

(b) Express the real quadratic polynomial as a product of its linear factors.

(3 marks)

|  |
| --- |
| **Solution** |
|  |
| **Specific behaviours** |
| ✓ complete square  ✓ express as difference of squares  ✓ write as required |

Question 2 (6 marks)

(a) A set of real numbers is given by . Clearly show that one of the numbers in the set is rational. (3 marks)

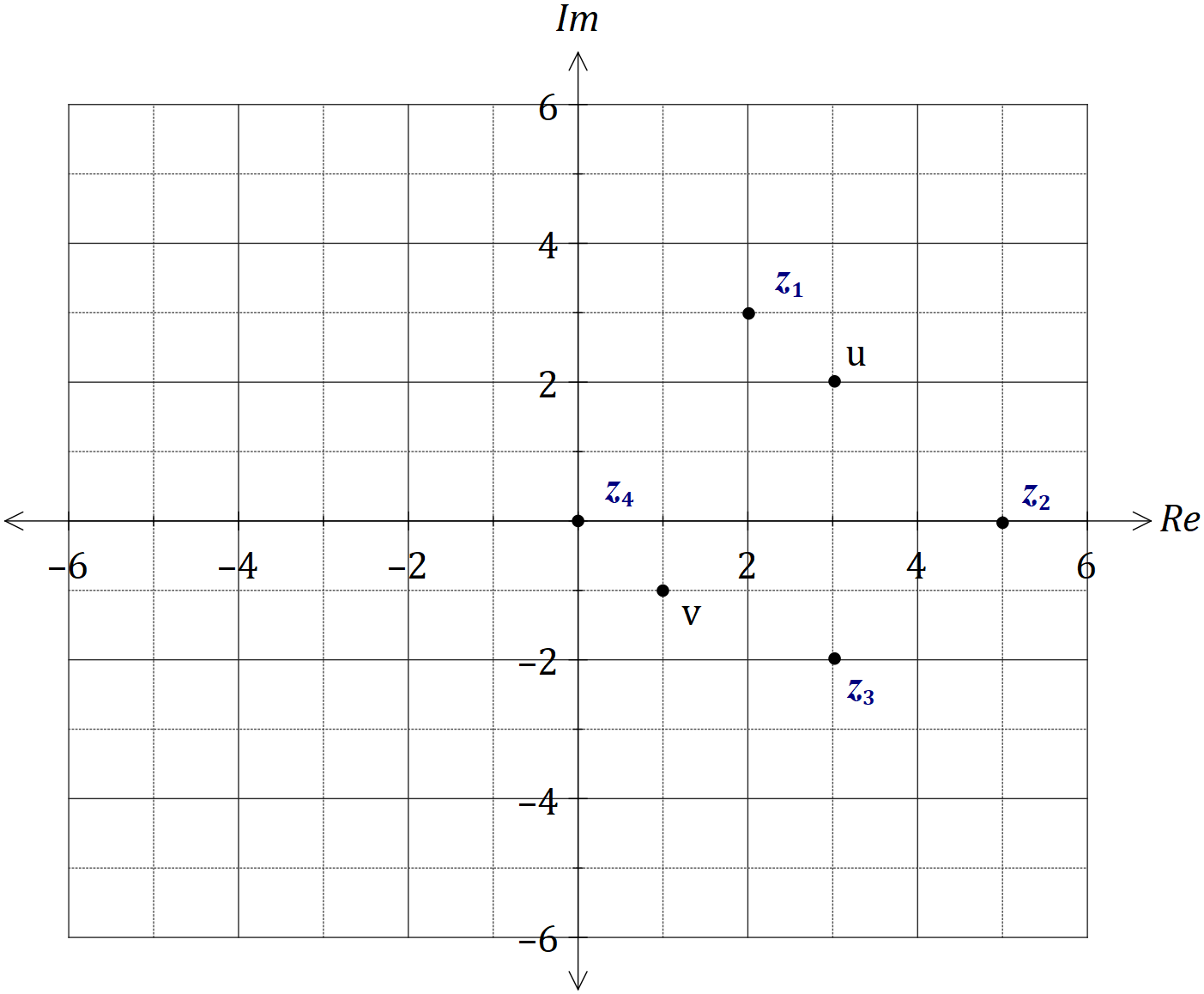
|  |
| --- |
| **Solution** |
|  |
| **Specific behaviours** |
| ✓ chooses rational number  ✓ indicates use of  ✓ writes as rational |

(b) Show that if is two more than a multiple of five, then will be one less than a multiple of five, where . (3 marks)

|  |
| --- |
| **Solution** |
|  |
| **Specific behaviours** |
| ✓ writes in required form  ✓ squares  ✓ writes in required form |

Question 3 (4 marks)

The complex numbers and are shown in the complex plane below.



Plot and label the following complex numbers:

(a) . (1 mark)

|  |
| --- |
| **Solution** |
| See graph |
| **Specific behaviours** |
| ✓  ✓  ✓  ✓ |

(b) . (1 mark)

(c) . (1 mark)

(d) . (1 mark)

Question 4 (8 marks)

Relative to the origin , the points , and have position vectors , and respectively.

(a) Determine in Cartesian form

(i) the vector . (1 mark)

|  |
| --- |
| **Solution** |
|  |
| **Specific behaviours** |
| ✓ subtracts position vectors |

(ii) a vector , parallel to and of magnitude . (3 marks)

|  |
| --- |
| **Solution** |
|  |
| **Specific behaviours** |
| ✓ states magnitude  ✓ indicates unit vector  ✓ states required vector (in either direction) |

(b) If , determine the values of the constants and . (4 marks)

|  |
| --- |
| **Solution** |
|  |
| **Specific behaviours** |
| ✓ uses coefficients to form equations  ✓ uses elimination or substitution  ✓ states  ✓ states |

Question 5 (9 marks)

Let and .

(a) Determine

|  |
| --- |
| **Solution** |
|  |
| **Specific behaviours** |
| ✓ multiple of  ✓ difference |

(i) . (2 marks)

(ii) . (2 marks)

|  |
| --- |
| **Solution** |
|  |
| **Specific behaviours** |
| ✓ at least two elements correct  ✓ all elements correct |

(iii) . (2 marks)

|  |
| --- |
| **Solution** |
|  |
| **Specific behaviours** |
| ✓ indicates use of determinant  ✓ correct inverse |

(b) Use a matrix method to solve the system of equations and .

(3 marks)

|  |
| --- |
| **Solution** |
|  |
| **Specific behaviours** |
| ✓ writes as matrix equation  ✓ shows correct use of inverse  ✓ states solution |

Question 6 (8 marks)

(a) Determine the acute angle in each of the following cases:

(i) . (2 marks)

|  |
| --- |
| **Solution** |
|  |
| **Specific behaviours** |
| ✓ uses complement  ✓ states angle |

(ii) . (2 marks)

|  |
| --- |
| **Solution** |
|  |
| **Specific behaviours** |
| ✓ sin in first quadrant  ✓ states angle |

(b) Prove that . (4 marks)

|  |
| --- |
| **Solution** |
|  |
| **Specific behaviours** |
| ✓ writes LHS as single fraction  ✓ multiplies by  ✓ uses Pythagorean identity  ✓ factorises denominator and simplifies |

Question 7 (5 marks)

Cyclic quadrilateral has diagonals and that intersect at . Given that cm, cm and cm, determine the smallest possible length of .

|  |
| --- |
| **Solution** |
|  |
| **Specific behaviours** |
| ✓ annotated diagram  ✓ expressions for and  ✓ uses intersecting chord theorem to form equation  ✓ factors equation  ✓ states required solution |

Question 8 (6 marks)

Let and be complex numbers such that and .

Determine and in the form , where .

|  |
| --- |
| **Solution** |
|  |
| **Specific behaviours** |
| ✓ eliminate  ✓ express as quotient  ✓ realise denominator  ✓ state  ✓ substitute for  ✓ state |

Additional working space

Question number: \_\_\_\_\_\_\_\_\_

© 2017 WA Exam Papers. John Curtin College of the Arts has a non-exclusive licence to copy and communicate this document for non-commercial, educational use within the school. No other copying, communication or use is permitted without the express written permission of WA Exam Papers. SN041-101-2.